

**Example 1.** Assume that you want to estimate the mean  $\mathbb{E}_{\mu^\dagger}[X]$  of some random variable  $X$  with respect to some unknown distribution  $\mu^\dagger$  on the interval  $[0, 1]$  based on the observation of  $n$  i.i.d. samples, given to finite resolution  $\delta$ , from the unknown distribution  $\mu^\dagger$ . The Bayesian answer to this problem is to assume that  $\mu^\dagger$  is the realization of some random measure distributed according to some prior  $\pi$  (i.e.  $\mu \sim \pi$ ) and then compute the posterior value of the mean by conditioning on the data. Now to specify the prior  $\pi$  you need to specify the distribution of all the moments of  $\mu$  (i.e. the distribution of the infinite dimensional vector  $(\mathbb{E}_\mu[X], \mathbb{E}_\mu[X^2], \mathbb{E}_\mu[X^3], \dots)$ ). So a natural way to assess the sensitivity of the Bayesian answer with respect to the choice of prior is to specify the distribution  $\mathbb{Q}$  of only a large, but finite, number of moments of  $\mu$  (i.e. specify the distribution of  $(\mathbb{E}_\mu[X], \mathbb{E}_\mu[X^2], \dots, \mathbb{E}_\mu[X^k])$  where  $k$  can be arbitrarily large). This defines a class of priors  $\Pi$  and our results show that no matter how large  $k$  is, no matter how large the number of samples  $n$  is, for any  $\mathbb{Q}$  that has a density with respect to the uniform distribution on the first  $k$  moments, if you observe the data at a fine enough resolution then the minimum and maximum of the posterior value of the mean over the class of priors  $\Pi$  are 0 and 1.